## Summary of research (Minoru Tabata)

- 1. **Partial differential equations and integro-partial differential equations studied in fluid dynamics.** Minoru Tabata proved the existence of local solutions to the Cauchy problem for the system of equations describing the motion of a mixture of compressible viscous and heat-conductive fluids. He proved decay of solutions to the Cauchy problem for the linearized Boltzmann equation with an external-force term and analyzed the point spectrum of the principal term of the equation.
- 2. Numerical analysis of agent-based models describing population movement. He constructed agentbased models describing an artificial society with population movement, developed a numerical method for the models. He numerically simulated Weidlich-Haag's theory of population movement and proved that the thermodynamic limit of the agent-based models is equal to a solution to Weidlich-Haag's master equation.
- 3. Numerical analysis of mathematical and statistical models using entropy. Using the maximum likelihood estimation method, he developed an error evaluation method for the relation between the communication capacity and the synchronization for spread spectrum communication.
- 4. A mathematical epidemiological model for human adult T-cell leukemia. To analyze epidemiological phenomena of human adult T-cell leukemia, in which the concentration of population in urban areas promotes the spread of infection, he constructed a mathematical epidemiological model with the effect of population concentration. He compared the numerical-simulation results with empirical data.
- 5. A nonlinear integro-partial differential equation in population dynamics. He proved the existence of local and global solutions of the master equation, a nonlinear integro-partial differential equation in population dynamics. He analyzed the asymptotic behavior of the solutions.
- 6. Nonlinear discrete equations with dual singular structure used in spatial economics. He proved the existence of short-run and long-run equilibria of the wage equation of Krugman's core-periphery model and constructed a numerical method for short-run equilibria. He applied Kakutani's fixed point theorem to Krugman's core-periphery model and applied the simulation results to spatial economics.
- 7. **Evolutionary game theory in spatial economics**. He proved the existence of global solutions to the replicator equation of evolutionary games in spatial economics, analyzed the asymptotic behavior of the global solutions, developed a numerical method for the solutions, and applied the results of numerical simulations to spatial economics.